

Algebra UNIT 7 Review of Types of Solving/Graphing

Solve by graphing. Identify the vertex, axis of symmetry, x-intercepts, and y-intercepts.

$$1.) y = -3x^2 + 6x + 5$$

vertex: $\frac{-b}{2a} = \frac{-6}{2(-3)} = \frac{-6}{-6} = 1$ (1, 8)

$$-3(1)^2 + 6(1) + 5 = 8$$

y-intercept = (0, 5)

x 3
y 4

$$2.) f(x) = x^2 + 4x + 3$$

vertex: $\frac{-b}{2a} = \frac{-4}{2(1)} = -2$ (-2, -1)

$$(-2)^2 + 4(-2) + 3 = -1$$

y intercept (0, 3)

x -1
y 0

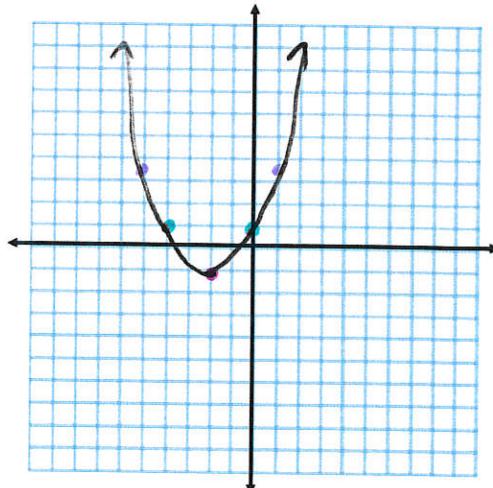
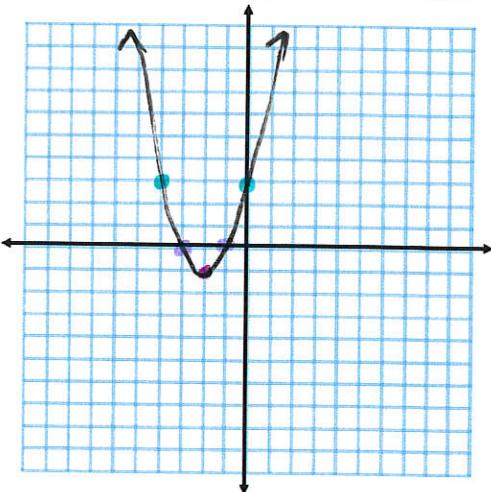
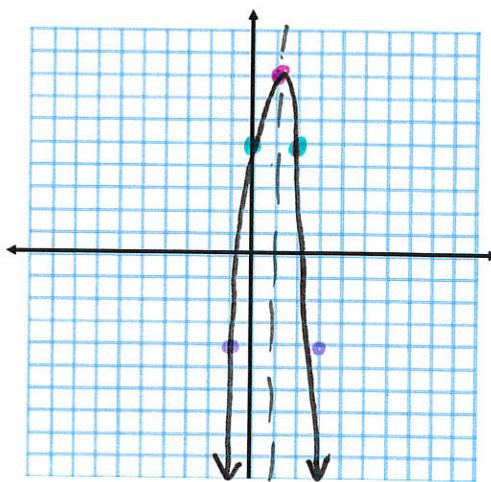
$$3.) y = \frac{1}{2}x^2 + 2x + 1$$

vertex: $\frac{-b}{2a} = \frac{-2}{2(\frac{1}{2})} = -2$ (-2, -1)

$$\frac{1}{2}(-2)^2 + 2(-2) + 1 = -1$$

y intercept (0, 1)

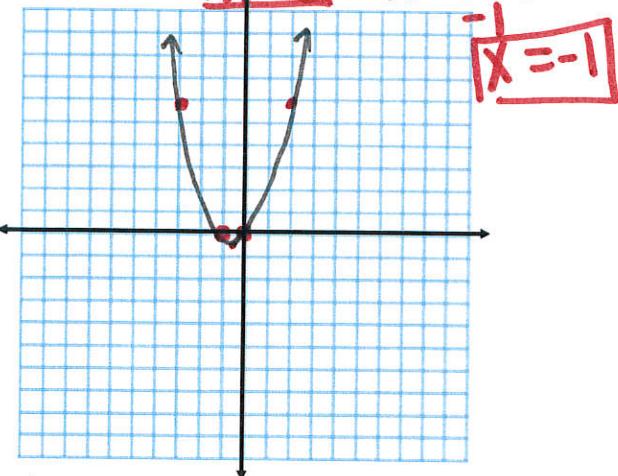
x 1
y 3.5



Solve by factoring. Identify the vertex, axis of symmetry, and find the zeroes. Then graph.

4.) $f(x) = x^2 + x$

$$\begin{aligned} x(x+1) &= 0 \\ (x=0) \quad x+1 &= 0 \end{aligned}$$



$$\frac{-b}{2a} = \frac{-1}{2}$$

$$\begin{array}{c|c} x & | 2 \\ \hline y & | 6 \end{array}$$

$$(-\frac{1}{2})^2 + -\frac{1}{2} = -\frac{1}{4}$$

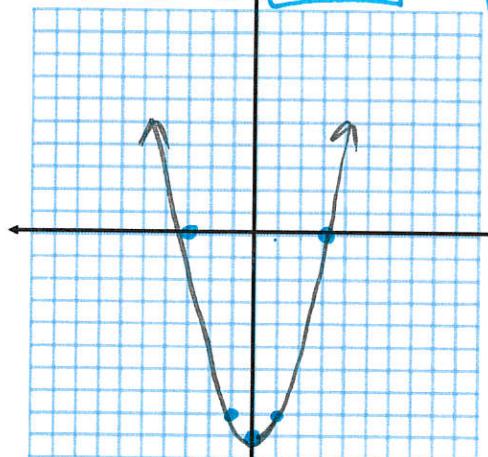
6.) $y = x^2 - 9$

$$(x+3)(x-3) = 0$$

$$x+3=0 \quad x-3=0$$

$$x=3 \quad x=-3$$

$$\begin{array}{c|c} x-3 & = 0 \\ \hline x & | 3 \end{array}$$



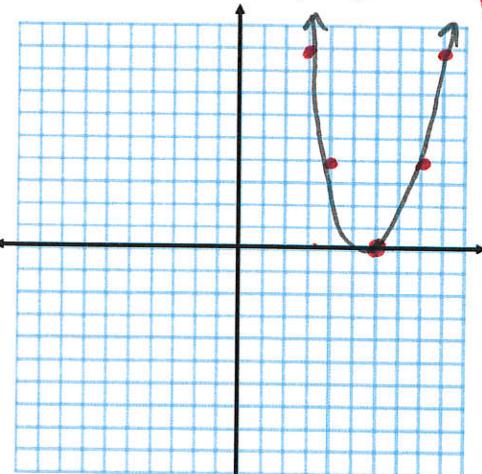
y-intercept $(0, -9)$

$$\begin{array}{c|c} x & | 1 \\ \hline y & | -8 \end{array}$$

5.) $y = x^2 - 12x + 36$

$$\begin{aligned} (x-6)(x-6) &= 0 \\ x-6 &= 0 \end{aligned}$$

$$x=6$$



$$\frac{-b}{2a} = \frac{12}{2} = 6$$

$$\begin{array}{c|c|c} x & | 4 & 3 \\ \hline y & | 4 & 9 \end{array}$$

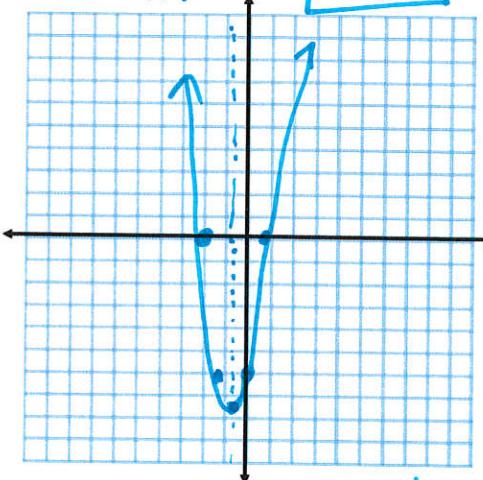
7.) $f(x) = 4x^2 + 5x - 6$

$$(x+2)(4x-3) = 0$$

$$x+2=0 \quad 4x-3=0$$

$$x=-2 \quad x=\frac{3}{4}$$

$$\begin{array}{c|c} 4x-3 & = 0 \\ \hline x & = \frac{3}{4} \end{array}$$



y-intercept $(0, -6)$

$$\begin{array}{l} \frac{-b}{2a} = \frac{-5}{2(4)} = \frac{-5}{8} \\ 4(-\frac{5}{8})^2 + 5(-\frac{5}{8}) - 6 \end{array}$$

$$\begin{array}{l} \text{vertex} \\ \left(-\frac{5}{8}, -1.5625\right) \end{array}$$

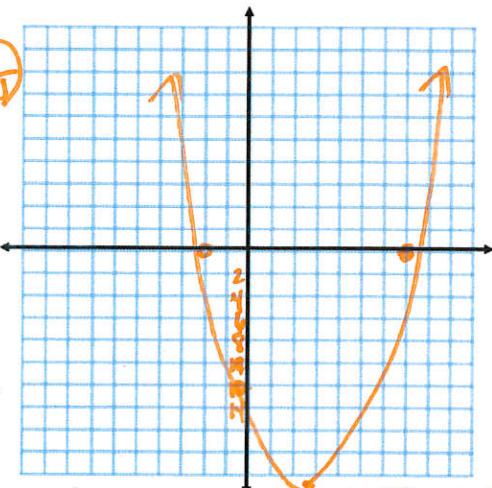
Solve by completing the square. Identify the vertex, axis of symmetry, and find the zeroes.

Then graph.

$$8.) \frac{2x^2 - 10x - 20 = 8}{2}$$

$$x^2 - 5x - 10 = 4$$

$$\frac{-b}{2a} = \frac{5}{2}$$



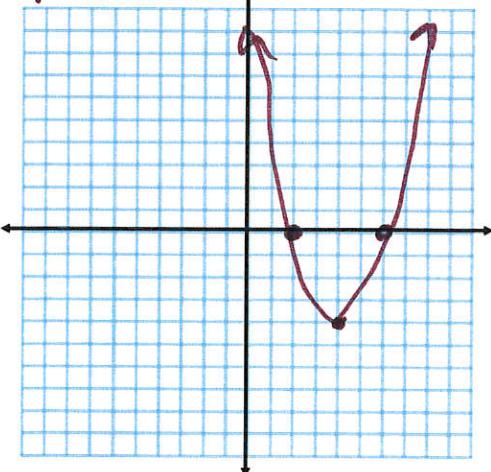
$$\begin{aligned} x^2 - 5x &= 14 \\ x^2 - 5x + 6.25 &= 20.25 \\ \sqrt{(x - \frac{5}{2})^2} &= \sqrt{20.25} \\ x - \frac{5}{2} &= \pm 4.5 \end{aligned}$$

$$\begin{aligned} x &= 7 \\ x &= -2 \\ x - \frac{5}{2} &= -4.5 \end{aligned}$$

$$10.) x^2 - 8x = -12$$

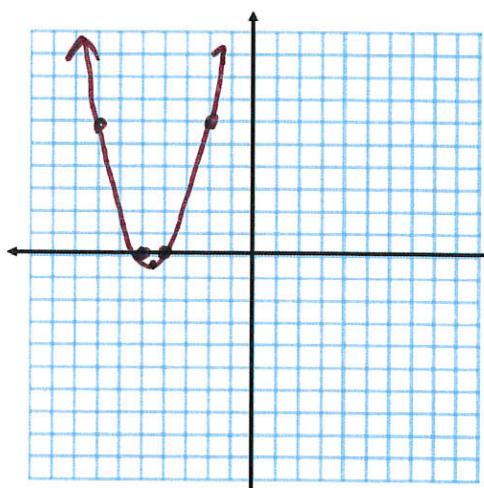
$$\begin{aligned} (\frac{b}{2})^2 &= (\frac{8}{2})^2 = 16 \\ x^2 - 8x + 16 &= 4 \\ (x - 4)^2 &= 4 \end{aligned}$$

$$\begin{aligned} x - 4 &= \pm 2 \\ x - 4 &= 2 & x = 6 \\ x - 4 &= -2 & x = 2 \end{aligned}$$



$$\begin{aligned} \frac{-b}{2a} &= \frac{8}{2(1)} = \frac{8}{2} = 4 \\ (4, -16) & \end{aligned}$$

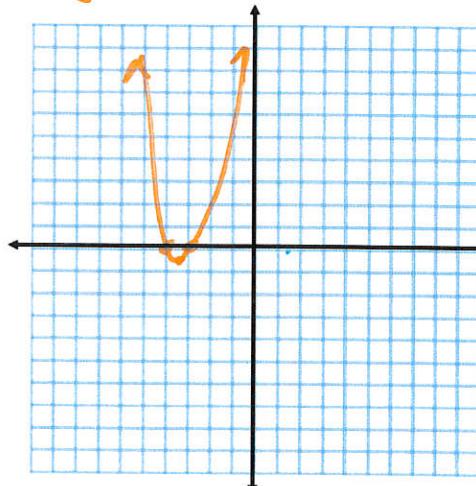
$$\begin{aligned} 9.) x^2 + 9x + 20 &= 0 \\ (\frac{b}{2})^2 &= (\frac{9}{2})^2 = 8.25 \\ x^2 + 9x + 20.25 &= 2.25 \\ \sqrt{(x + 4.5)^2} &= \sqrt{2.25} \\ x + 4.5 &= \pm 1.5 \end{aligned}$$



$$\begin{aligned} \frac{-b}{2a} &= \frac{-9}{2} = -4.5 & (-4.5, -2.25) \\ \frac{x+2}{6} & \end{aligned}$$

$$11.) y = x^2 + 7x + 12$$

$$\begin{aligned} -12 &= x^2 + 7x \\ 0.25 &= x^2 + 7x + 12.25 \\ 0.25 &= (x + 3.5)^2 \end{aligned}$$



$$\begin{aligned} \frac{-b}{2a} &= \frac{-7}{2(1)} = -3.5 \\ (-3.5, -0.25) & \end{aligned}$$